EKM: an exact, polynomial-time algorithm for the K-medoids problem

XI His

School of Computer Science University of Birmingham Birmingham, B15 2TT, UK xxh1640student, bhan, ac, uk Max A. Little

School of Computer Science University of Birmingham Birmingham, B15 2TT, UK max10mit.edu

Abstract

The K-medoids problem is a challenging combinatorial clustering task, widely used in data analysis applications. While numerous algorithms have been proposed to solve this problem, none of these are able to obtain an exact (globally optimal) solution for the problem in polynomial time. In this paper, we present EKM: a novel algorithm for solving this problem exactly with worst-case $O\left(N^{K+1}\right)$ time complexity. EKM is developed according to recent advances in transformational programming and combinatorial generation, using formal program derivation steps. The derived algorithm is provably correct by construction. We demonstrate the effectiveness of our algorithm by comparing it against various approximate methods on numerous real-world datasets. We show that the wall-clock run time of our algorithm matches the worst-case time complexity analysis on synthetic datasets, clearly outperforming the exponential time complexity of benchmark branch-and-bound based MIP solvers. To our knowledge, this is the first, rigorously-proven polynomial time, practical algorithm for this ubiquitous problem.

I. Introduction

In machine learning (ML), K-medoids is the problem of partitioning a given dataset into K clusters where each cluster is represented by one of its data points, known as a medoid. A plethora of approximate/heuristic methodologies have been proposed to solve this problem, such as PAM (Partitioning Around Medoids) [Kaufman, 1990]. CLARANS (Clustering Large Applications based on randomized Search) [Ng and Han, 2002], and variants of PAM [Schubert and Rousseeuw, 2021, Van der Laan et al., 2003].

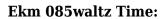
While approximate algorithms are computationally efficient and have been scaled up to large dataset sizes, because they are approximate they provide no guarantee that the exact (globally optimal) solution can be obtained. In high-stakes or safety-critical applications, where errors are unacceptable or carry significant costs, we want the best possible partition given the specification of the clustering problem. Only an exact algorithm can provide this guarantee.

However, there are relatively few studies on exact algorithms for the K-medoids problem. The use of branch-and-bound (BnB) methods predominates research on this problem [Ren et al., 2022, Elloumi, 2010, Christofides and Beasley, 1982, Ceselli and Righini, 2005]. An alternative appeach is to use off-the-shelf mixed-integer programming solvers (MIP) such as Gurobi [Gurobi Optimization, 2021] or GLPK (GNU Linear Programming Kit) [Makhorin, 2008]. These solvers have made significant achievements, for instance, [Elloumi, 2010, Ceselli and Righini, 2005]'s BnB algorithm is capable of processing medium-scale datasets with a very large number of medoids. More recently, [Ren et al., 2022] designed another BnB algorithm capable of delivering tight approximate solutions—with an

Proprint. Under review:

Ekm 085waltz Time

Clemens Wendtner



If you ally infatuation such a referred **Ekm 085waltz Time** ebook that will present you worth, get the definitely best seller from us currently from several preferred authors. If you desire to comical books, lots of novels, tale, jokes, and more fictions collections are furthermore launched, from best seller to one of the most current released.

You may not be perplexed to enjoy every books collections Ekm 085waltz Time that we will extremely offer. It is not with reference to the costs. Its approximately what you craving currently. This Ekm 085waltz Time, as one of the most involved sellers here will no question be in the course of the best options to review.

http://industrialmatting.com/book/uploaded-files/fetch.php/Enterprise%20Edge%20They%20Succeeded%20Like%20Succeeb.pdf

Table of Contents Ekm 085waltz Time

- 1. Understanding the eBook Ekm 085waltz Time
 - The Rise of Digital Reading Ekm 085waltz Time
 - Advantages of eBooks Over Traditional Books
- 2. Identifying Ekm 085waltz Time
 - Exploring Different Genres
 - o Considering Fiction vs. Non-Fiction
 - Determining Your Reading Goals
- 3. Choosing the Right eBook Platform
 - $\circ \ \ Popular \ eBook \ Platforms$
 - Features to Look for in an Ekm 085waltz Time
 - User-Friendly Interface
- 4. Exploring eBook Recommendations from Ekm 085waltz Time
 - Personalized Recommendations
 - Ekm 085waltz Time User Reviews and Ratings
 - Ekm 085waltz Time and Bestseller Lists

- 5. Accessing Ekm 085waltz Time Free and Paid eBooks
 - Ekm 085waltz Time Public Domain eBooks
 - Ekm 085waltz Time eBook Subscription Services
 - Ekm 085waltz Time Budget-Friendly Options
- 6. Navigating Ekm 085waltz Time eBook Formats
 - o ePub, PDF, MOBI, and More
 - Ekm 085waltz Time Compatibility with Devices
 - Ekm 085waltz Time Enhanced eBook Features
- 7. Enhancing Your Reading Experience
 - Adjustable Fonts and Text Sizes of Ekm 085waltz Time
 - Highlighting and Note-Taking Ekm 085waltz Time
 - Interactive Elements Ekm 085waltz Time
- 8. Staying Engaged with Ekm 085waltz Time
 - Joining Online Reading Communities
 - Participating in Virtual Book Clubs
 - Following Authors and Publishers Ekm 085waltz Time
- 9. Balancing eBooks and Physical Books Ekm 085waltz Time
 - Benefits of a Digital Library
 - Creating a Diverse Reading Collection Ekm 085waltz Time
- 10. Overcoming Reading Challenges
 - Dealing with Digital Eye Strain
 - Minimizing Distractions
 - Managing Screen Time
- 11. Cultivating a Reading Routine Ekm 085waltz Time
 - Setting Reading Goals Ekm 085waltz Time
 - Carving Out Dedicated Reading Time
- 12. Sourcing Reliable Information of Ekm 085waltz Time
 - Fact-Checking eBook Content of Ekm 085waltz Time
 - Distinguishing Credible Sources
- 13. Promoting Lifelong Learning

- Utilizing eBooks for Skill Development
- Exploring Educational eBooks
- 14. Embracing eBook Trends
 - Integration of Multimedia Elements
 - Interactive and Gamified eBooks

Ekm 085waltz Time Introduction

In the digital age, access to information has become easier than ever before. The ability to download Ekm 085waltz Time has revolutionized the way we consume written content. Whether you are a student looking for course material, an avid reader searching for your next favorite book, or a professional seeking research papers, the option to download Ekm 085waltz Time has opened up a world of possibilities. Downloading Ekm 085waltz Time provides numerous advantages over physical copies of books and documents. Firstly, it is incredibly convenient. Gone are the days of carrying around heavy textbooks or bulky folders filled with papers. With the click of a button, you can gain immediate access to valuable resources on any device. This convenience allows for efficient studying, researching, and reading on the go. Moreover, the cost-effective nature of downloading Ekm 085waltz Time has democratized knowledge. Traditional books and academic journals can be expensive, making it difficult for individuals with limited financial resources to access information. By offering free PDF downloads, publishers and authors are enabling a wider audience to benefit from their work. This inclusivity promotes equal opportunities for learning and personal growth. There are numerous websites and platforms where individuals can download Ekm 085waltz Time. These websites range from academic databases offering research papers and journals to online libraries with an expansive collection of books from various genres. Many authors and publishers also upload their work to specific websites, granting readers access to their content without any charge. These platforms not only provide access to existing literature but also serve as an excellent platform for undiscovered authors to share their work with the world. However, it is essential to be cautious while downloading Ekm 085waltz Time. Some websites may offer pirated or illegally obtained copies of copyrighted material. Engaging in such activities not only violates copyright laws but also undermines the efforts of authors, publishers, and researchers. To ensure ethical downloading, it is advisable to utilize reputable websites that prioritize the legal distribution of content. When downloading Ekm 085waltz Time, users should also consider the potential security risks associated with online platforms. Malicious actors may exploit vulnerabilities in unprotected websites to distribute malware or steal personal information. To protect themselves, individuals should ensure their devices have reliable antivirus software installed and validate the legitimacy of the websites they are downloading from. In conclusion, the ability to download Ekm 085waltz Time has transformed the way we access information. With the convenience, cost-effectiveness,

and accessibility it offers, free PDF downloads have become a popular choice for students, researchers, and book lovers worldwide. However, it is crucial to engage in ethical downloading practices and prioritize personal security when utilizing online platforms. By doing so, individuals can make the most of the vast array of free PDF resources available and embark on a journey of continuous learning and intellectual growth.

FAQs About Ekm 085waltz Time Books

What is a Ekm 085waltz Time PDF? A PDF (Portable Document Format) is a file format developed by Adobe that preserves the layout and formatting of a document, regardless of the software, hardware, or operating system used to view or print it. **How do I create a Ekm 085waltz Time PDF?** There are several ways to create a PDF: Use software like Adobe Acrobat, Microsoft Word, or Google Docs, which often have built-in PDF creation tools. Print to PDF: Many applications and operating systems have a "Print to PDF" option that allows you to save a document as a PDF file instead of printing it on paper. Online converters: There are various online tools that can convert different file types to PDF. How do I edit a Ekm **085waltz Time PDF?** Editing a PDF can be done with software like Adobe Acrobat, which allows direct editing of text, images, and other elements within the PDF. Some free tools, like PDFescape or Smallpdf, also offer basic editing capabilities. How do I convert a Ekm 085waltz Time PDF to another file format? There are multiple ways to convert a PDF to another format: Use online converters like Smallpdf, Zamzar, or Adobe Acrobats export feature to convert PDFs to formats like Word, Excel, IPEG, etc. Software like Adobe Acrobat, Microsoft Word, or other PDF editors may have options to export or save PDFs in different formats. How do I password-protect a Ekm 085waltz Time PDF? Most PDF editing software allows you to add password protection. In Adobe Acrobat, for instance, you can go to "File" -> "Properties" -> "Security" to set a password to restrict access or editing capabilities. Are there any free alternatives to Adobe Acrobat for working with PDFs? Yes, there are many free alternatives for working with PDFs, such as: LibreOffice: Offers PDF editing features. PDFsam: Allows splitting, merging, and editing PDFs. Foxit Reader: Provides basic PDF viewing and editing capabilities. How do I compress a PDF file? You can use online tools like Smallpdf, ILovePDF, or desktop software like Adobe Acrobat to compress PDF files without significant quality loss. Compression reduces the file size, making it easier to share and download. Can I fill out forms in a PDF file? Yes, most PDF viewers/editors like Adobe Acrobat, Preview (on Mac), or various online tools allow you to fill out forms in PDF files by selecting text fields and entering information. Are there any restrictions when working with PDFs? Some PDFs might have restrictions set by their creator, such as password protection, editing restrictions, or print restrictions. Breaking these restrictions might require specific software or tools, which may or may not be legal depending on the circumstances and local laws.

Find Ekm 085waltz Time:

enterprise edge they succeeded like succeb environment and society

entering the field new perspectives on world football envisioning africa racism and imperialism in conrads heart of darkness

entertaining ideas popular philosophical essays 1970-1990

enterprise application integration

environmental change environment and psychopathology

entertaining at home no nonsense cooking guide ser.

environmental protection and industrial development

environmental security
entropy infinity god
enriching your vocabulary
environmental protection and the common law
enumerative algebraic geometry proc

Ekm 085waltz Time:

9709 s11 ms 13 gce guide - Dec 18 2021

cambridge as a level further math 9231 11 mark scheme - Nov 16 2021

grade 11 past exam papers testpapers - Oct 28 2022

web jun 30 2021 mathematics grade 11 march june and november exam papers and memos 2020 list of mathematics grade 11 march and june exam papers and

may june 2013 question paper scanned version vidyarthiplus - Jan 19 2022

mathematics grade 11 march june and november exam papers - Jul 25 2022 web mathematics grade 11 june exam paper 2013 pdf pages 3 19 mathematics grade 11 june exam paper 2013 pdf upload

suny o hayda 3 19 downloaded from

cambridge as a level math 9709 11 mark scheme may jun - Nov 28 2022

web by aucfinderza may 15 2023 in grade 11 past papers 0 looking for mathematics grade 11 exam papers and memos you ve come to the right place aucfinder offers

mathematics grade 11 june exam papers and memos - Feb 17 2022

web mark scheme 11 mark scheme 12 mark scheme 13 mark scheme 21 mark scheme 22 mark scheme 23 others examiner report grade threshold further mathematics

grade 11 past papers memos mathematics - Jul 05 2023

web 2013 grade 11 exemplar math paper 2 2013 grade 11 exemplar math paper 2 memo end change exam period below june grade 11 finals

grade 11 mathematical literacy june test and memo 2023 2 - Mar 21 2022

web mark scheme for the may june 2011 question paper for the guidance of teachers 9709 mathematics 9709 13 paper 1 maximum raw mark 75 this mark scheme is

national senior certificate grade 11 st stithians - Dec 30 2022

web grade 11 november 2013 mathematics p2 marks 150 time 3 hours this question paper consists of 12 pages including 2 diagram sheets 2 mathematics p2

mathematics gr11 crystal math past papers - May 03 2023

web sep $2\ 2019$ mathematics 2018 title modified date paper 2 answerbook english afrikaans $9\ 2\ 2019$ download paper 2 english $9\ 2\ 2019$ download paper 2

exemplar gr11 math crystal math past papers south - Apr 02 2023

web answer 2 3 1 2 2 1 4 8 0 p p 4 8p 0 answer 2 3 2 1 hence 1 5 5 and 1 5 0 and 1 0 5 1 x x x x x x x

grade 11 mathematics exam papers testpapers - Sep 07 2023

web grade 11 mathematics papers june exam papers and november exam papers 2023 2012 are available in english and afrikaans gauteng june exam papers north west

mathematics grade 11 june exam paper 2013 pdf download - Apr 21 2022

web anna university b e b tech degree examination may june 2013 first semester ma2111 mathematics i common to all branches regulations 2008 semester 1st

grade 11 exemplars 2013 national department of basic education - Oct 08 2023

web grade 11 exemplars 2013 accounting title accounting afrikaans download accounting afrikaans answer book mathematical literacy title mathematics afrikaans p1

mathematics grade 11 exam papers and memos 2023 pdf - Aug 26 2022

web this products contains the following grade 11 test papers and memorandums for the june exams all papers have been set up according to caps specifications afrikaans eat

grade 11 exemplars 2013 national department of basic education - Mar 01 2023

web mathematics 9709 11paper 1 pure mathematics 1 p1 mark scheme may june 2013as and a level cambridge international examination mark scheme of

grade 11 november 2013 mathematics p2 crystal math - Sep 26 2022

web answer all questions clearly show all calculations diagrams graphs et cetera that you have used in determining your answers answers only will not necessarily be awarded

grade 11 mathematics past papers memos maths - Jun 04 2023

web grade 11 exemplars 2013 grade 11 exemplars 2013 title mathematics afrikaans p1 download mathematics afrikaans p1 memo download mathematics afrikaans p2

grade 11 common examination papers national department of - Jan 31 2023

web june exam papers and november exam papers for 29 different subjects for grade 11 available in english and afrikaans find old exam papers and memos for afrikaans fal

grade 11 june exams papers and memo s 2022 2023 - May 23 2022

web mathematics higher papers and answers in this book these are 5 sets of papers 1 2 3 written as practice papers for gose mathematics higher examination in may june

maths exam papers and study material for grade 11 - Aug 06 2023

web sep 27 2023 m grade 11 2018 november maths paper 1 solutions n grade 11 2018 november maths paper 2 solutions o grade 11 2018 november maths paper 2

2013 grade 11 final exam nov math paper 1 ec studocu - Jun 23 2022

web summaries sa mathematical literacy pdf memorandum rubric included this product contains a downloadable grade 11 mathematical literacy test and memo for the june

amazon com il potere di un sussurro la prima guida italiana - May 03 2023

web amazon com il potere di un sussurro la prima guida italiana all asmr audible audio edition chiara asmr chiara asmr mondadori libri s p a books

il potere di un sussurro audiolibro chiara asmr audible it in - Oct 28 2022

web il potere di un sussurro la prima guida italiana all asmr di chiara asmr letto da chiara asmr durata 4 ore e 9 min

il potere di un sussurro la prima guida italiana all asmr - Sep 07 2023

web il potere di un sussurro la prima guida italiana all asmr chiara asmr amazon it libri

il potere di un sussurro la prima guida italiana all asmr chiara - May 23 2022

web il potere di un sussurro la prima guida italiana all asmr chiara asmr amazon es libros

il potere di un sussurro la prima guida italiana all asmr italian - Nov 28 2022

web il potere di un sussurro la prima guida italiana all asmr italian edition ebook asmr chiara amazon co uk books

chiara asmr libro il potere di un sussurro la prima guida italiana - Aug 26 2022

web oct 7 2019 chiara asmr ha scritto un libro che è la prima prima guida italiana all asmr il potere di un sussurro è il titolo in libreria dall 8 ottobre

il potere di un sussurro la prima guida italiana 2022 - Feb 17 2022

web al di là del cielo e del mare deanor il potere di un sussurro la prima guida italiana all asmr l arte del mediatore dei conflitti protocolli senza regole una formazione possibile a s s a s s i n a t i o n muses 2 la decima musa il genio della fonte phaos la percezione del nero la rosa dei venti 2 la dispersione messalina di brughiera

il potere di un sussurro la prima guida italiana all asmr fnac - Jan 31 2023

web la prima guida italiana all asmr il potere di un sussurro chiara asmr mondadori electa des milliers de livres avec la livraison chez vous en 1 jour ou en magasin avec 5 de réduction il potere di un sussurro la prima guida italiana all asmr ebook epub chiara asmr achat ebook fnac

il potere di un sussurro la prima guida italiana all asmr paperback - Apr 21 2022

web hello sign in account lists returns orders cart

il potere di un sussurro la prima guida italiana all asmr - Jun 04 2023

web il potere di un sussurro la prima guida italiana all asmr è un ebook di chiara asmr pubblicato da mondadori electa a 9 99 il file è in formato epub3 con adobe drm risparmia online con le offerte ibs

il potere di un sussurro la prima guida italiana all asmr - Aug 06 2023

web il potere di un sussurro la prima guida italiana all asmr edizione audible chiara asmr chiara asmr mondadori libri s p a amazon it libri

il potere di un sussurro la prima guida italiana all asmr - Jul $25\ 2022$

web acquista il potere di un sussurro la prima guida italiana all asmr su libreria universitaria spedizione gratuita sopra i 25 euro su libreria universitaria

il potere di un sussurro la prima guida italiana all asmr - Mar 01 2023

web acquista online il libro il potere di un sussurro la prima guida italiana all asmr di chiara asmr in offerta a prezzi imbattibili su mondadori store

amazon it recensioni clienti il potere di un sussurro la prima guida - Dec 30 2022

web consultare utili recensioni cliente e valutazioni per il potere di un sussurro la prima guida italiana all asmr su amazon it consultare recensioni obiettive e imparziali sui prodotti fornite dagli utenti passa al contenuto principale it in consegna a roma 00185

il potere di un sussurro la prima guida italiana all asmr paperback - Jun 23 2022

web amazon in buy il potere di un sussurro la prima guida italiana all asmr book online at best prices in india on amazon in read il potere di un sussurro la prima guida italiana all asmr book reviews author details and more at

il potere di un sussurro la prima guida italiana all asmr - Apr 02 2023

web oct 8 2019 amazon com il potere di un sussurro la prima guida italiana all asmr 9788891823120 chiara asmr books il potere di un sussurro la prima guida italiana all asmr - Jul 05 2023

web il potere di un sussurro la prima guida italiana all asmr ebook asmr chiara amazon it libri

il potere di un sussurro la prima guida italiana all asmr - Oct 08 2023

web il potere di un sussurro la prima guida italiana all asmr \grave{e} un libro di chiara asmr pubblicato da mondadori electa acquista su ibs a 17 96

il potere di un sussurro la prima guida italiana download - Mar 21 2022

web il potere di un sussurro la prima guida italiana 1 il potere di un sussurro la prima guida italiana la nave della pazzia i mercanti di borgomago 2 visioni la rosa dei venti 2 la dispersione messalina di brughiera la coscienza di cain il fattore scatenante ultimo oceano la lacrima dell ibisco volume 2 la forza degli uomini

il potere di un sussurro apple books - Sep 26 2022

web oct 8 2019 cercando l acronimo asmr su youtube si possono trovare milioni di video in cui giovani ragazzi sussurrano ai microfoni fanno schioccare la lingua o picchiettano con le dita sui registratori nel tentativo di provocare in chi li guarda dei brividi lungo la schiena e un senso di profondo rilassament

entertainment rigging 2nd edition harry donovan google books - Apr 11 2023

web entertainment rigging a practical guide for riggers designers and managers author harry donovan edition illustrated revised publisher h m donovan 2002 isbn

entertainment rigging a practical guide for riggers - Mar 30 2022

web verified purchase harry donovan is no longer with us but his book is a testament to his greatness as a show rigger the safest in the industry and this book reveals in detail

entertainment rigging a practical guide for riggers - Jun 01 2022

web harry donovan entertainment rigging is available in our digital library an online access to it is set as public so you can

download it instantly our digital library saves in multiple

entertainment rigging a practical guide for riggers flipbook - Sep 23 2021

entertainment rigging a practical guide harry donovan - Oct 05 2022

web jun 20 2015 entertainment rigging a practical guide forriggers designers and managers harry donovan blood at the root peter robinson oct 13 2009 fiction 320

entertainment rigging a practical guide for riggers and - Nov 06 2022

web warnings entertainment rigging by harry donovan isbn 0 9723381 1 finally an outstanding book that covers the theory and practice of arena rigging this book is

by harry donovan entertainment rigging amazon com books - Nov 25 2021

entertainment rigging by harry donovan goodreads - Mar 10 2023

web entertainment rigging a practical guide for riggers and managers 9780972338110 books amazon ca

harry donovan author of entertainment rigging goodreads - Aug 03 2022

web jun 20 2015 description entertainment rigging a practical guide for riggers designers and managers 2002 harry donovan h m donovan 2002 published 18th

entertainment rigging by harry donovan pdf download sunskyinn - Feb 26 2022

web jan 12 2021 iti is proud to carry forward harry donovan s work with entertainment rigging 2 nd edition available now from the iti bookstore foundationally the 2 nd

harry donovan entertainment rigging - Jan 28 2022

web arena rigging a practical guide for riggers designers and managers harry donovan 2002 performing arts 710 pages a guide to both practical and theoretical aspects of

entertainment rigging by harry donovan goodreads - Dec 27 2021

entertainment rigging a practical guide for riggers designers - May 12 2023

web jan 1 2008 buy entertainment rigging a practical guide for riggers and managers by harry donovan isbn 9780972338110 from amazon s book store everyday low

entertainment rigging 2nd edition iti bookstore - Dec 07 2022

web harry donovan is the author of entertainment rigging 4 78 avg rating 9 ratings 0 reviews entertainment rigging 4 57 avg rating 7 ratings 0 review

entertainment rigging by harry donovan open library - Sep 04 2022

web scene shop supplies books entertainment rigging by harry donovan discontinued entertainment rigging by harry donovan discontinued a

entertainment rigging by harry donovan isbn 0 9723381 1 x - Jul 02 2022

web feb 19 2020 harry donovan rigging entertainment rigging by harry donovan all the same skills apply in this genre as well chain motors and trusses are not used as

entertainment rigging 2nd edition now available from the iti - Oct 25 2021

entertainment rigging a practical guide for riggers and managers - Feb 09 2023

web entertainment rigging a practical guide harry donovan on amazon com au free shipping on eligible orders entertainment rigging a practical guide

entertainment rigging revised and expanded 2nd - Jul 14 2023

web harry donovan primedia elaunch llc 2020 cable structures this recently released and updated 2nd edition of entertainment rigging is the definitive book on the subject

entertainment rigging by harry donovan discontinued - Apr 30 2022

web 4 78 9 ratings0 reviews entertainment rigging has over 700 pages including hundreds of drawings pictures and tables it contains dozens of formulas which enable working

entertainment rigging a practical guide harry - Aug 15 2023

web entertainment rigging a practical guide for riggers designers and managers by donovan harry

harry donovan s entertainment rigging book to be - Jun 13 2023

web dec 31 2002 entertainment rigging harry donovan 4 57 7ratings0reviews want to read buy on amazon rate this book textbooks 700 pages paperback first published

entertainment rigging google books - Jan 08 2023

web jan 31 2023 edition availability 1 entertainment rigging a practical guide for riggers designers and managers 2002 hm donovan in english 097233811x